

# **Angle-Resolved Ion Charge State Distribution Measurements in a Vacuum Arc Plasma Using Time-of- Flight Mass Spectroscopy**

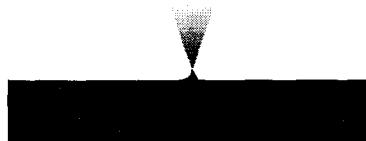
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Jet Propulsion Laboratory  
California Institute of Technology



# Cathode Spots in Vacuum Arcs Create Extreme Plasma Environments

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## Vacuum Arc Electron Emission Processes



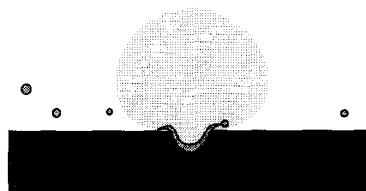
### Site Initiation

Field emission from micropoint or dielectric inclusion.



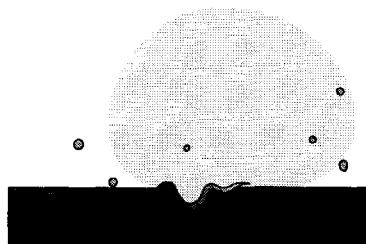
### Explosive Evaporation

Excessive joule heating in micro-emission site generates plasma by explosive vaporization.



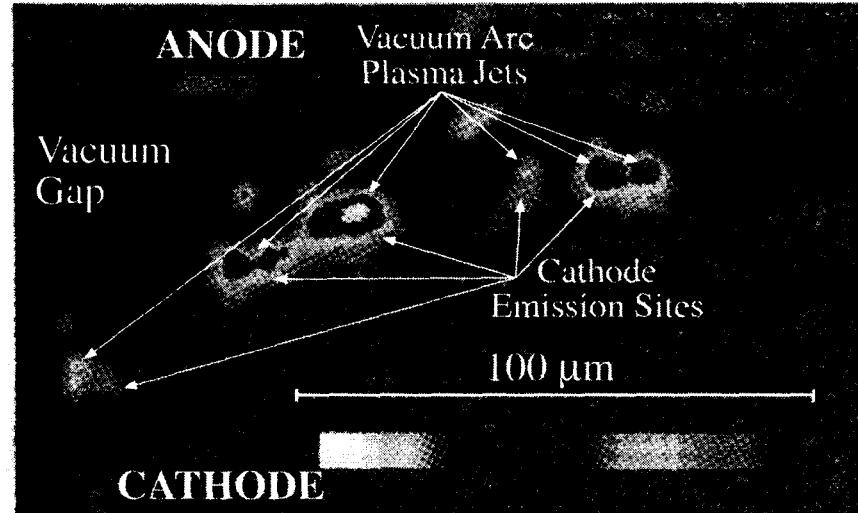
### Crater Formation

Power deposited by joule heating and ion bombardment heats surface to extreme temperatures. Electrons emitted by thermal-field emission.



### New Site Formation

Decreasing power density leads to site extinction and field emission at a nearby micropoint causes spot to shift.



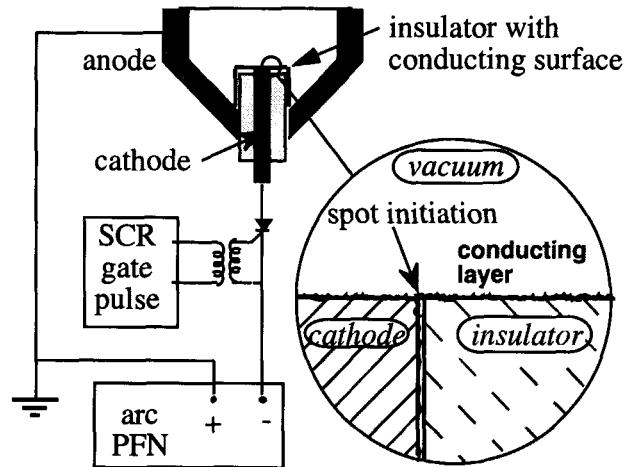
Laser absorption image shows ultra-high density plasma plumes created by cathode emission sites in a vacuum arc

- Vacuum arcs generate environments with unique properties
  - Current densities of  $10^8 \text{ A/cm}^2$
  - Surface heat fluxes of  $10^8\text{--}10^9 \text{ W/cm}^2$
  - Plasma densities of  $10^{20}\text{--}10^{21} \text{ cm}^{-3}$  (nearly the density of the solid metal!)
  - Nearly 100% ionization of metal vapor
  - Plasma expansion velocities of  $10^4 \text{ m/s}$
- Pressure ionization, not electron bombardment processes, creates plasma efficiently in a tiny volume

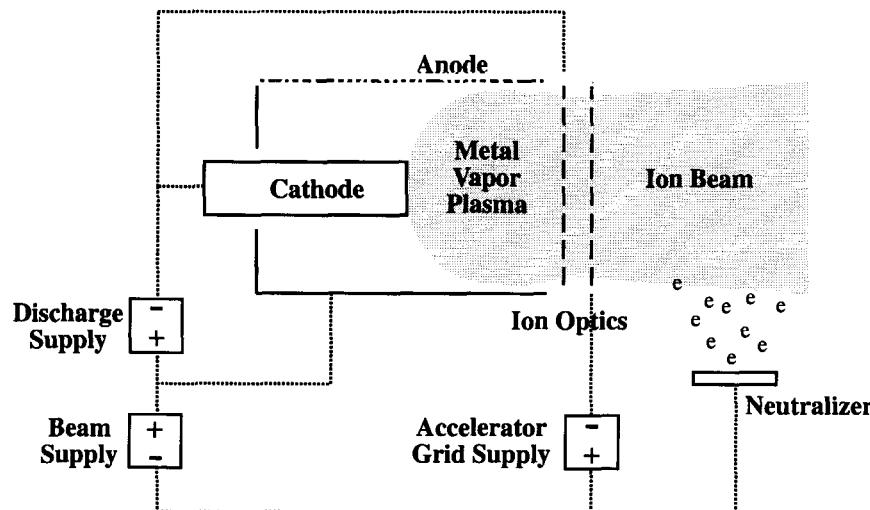


# Exploiting Extreme Conditions in Vacuum Arc Plasmas for Propulsion

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Schematic of a vacuum arc thruster



Schematic of a vacuum arc ion thruster

## CONCEPT

Metal vapor plasmas can be used to produce thrust in several ways

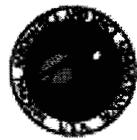
- Direct thrust from plasma plume expansion
- Electrostatic or electromagnetic acceleration of the dense plasma

## ADVANTAGES

- Vacuum arc plasma sources provide unique scaling advantages
  - No magnetic field required to confine or generate plasma
  - Plasma is created in small volume
  - No gas feed system is required
  - Discharge current can be tailored to produce wide range of plasma densities
- Plasma plume expansion allows higher current density extraction through ion optics

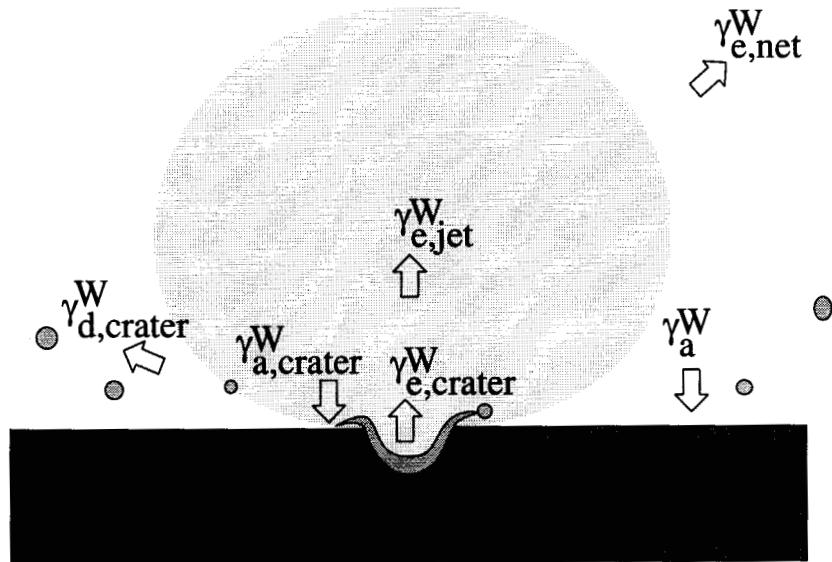
## APPLICATIONS

- Miniaturized thrusters for microspacecraft applications
- Very high density plasmas may enable very high power thrusters



# Regularities in Vacuum Arc Discharges Make Simple Performance Models Possible

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- Mass loss scales with discharge current

$$\dot{m}_t = E_r J_d,$$

- Ion current is proportional to discharge current

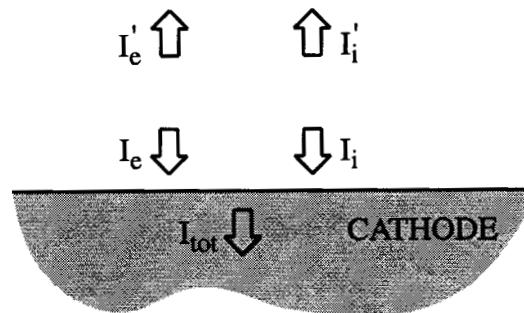
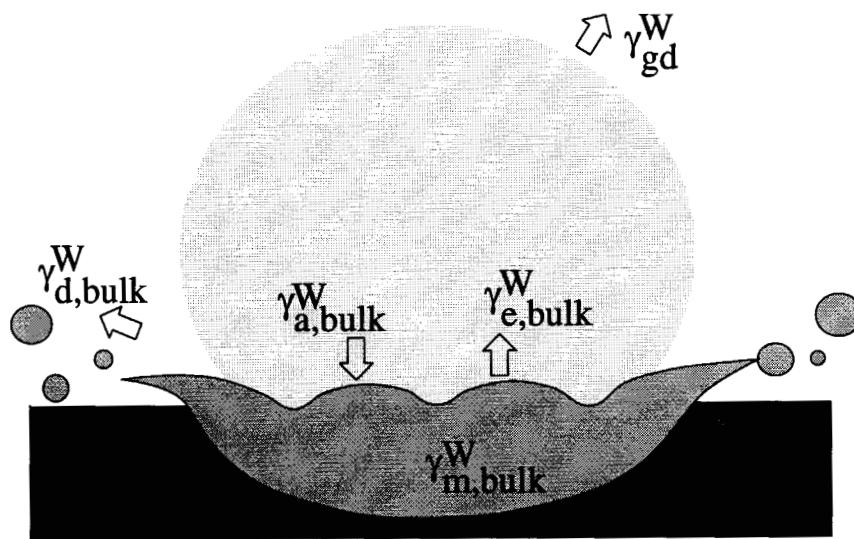
$$J_i = \sum_Z J_Z = f_i J_d$$

- Experiments show that  $f_i$  is typically 0.07-0.1
- Ion mass loss fraction depends on  $f_i$  and  $E_r$

$$\dot{m}_i = \sum_Z \frac{J_Z M_i}{Ze} = \frac{f_i J_d M_i}{e} \langle Z^{-1} \rangle,$$

$$\langle Z^{-1} \rangle = \sum_Z \frac{f_Z}{Z}. \quad f_Z = \frac{J_Z}{J_i}.$$

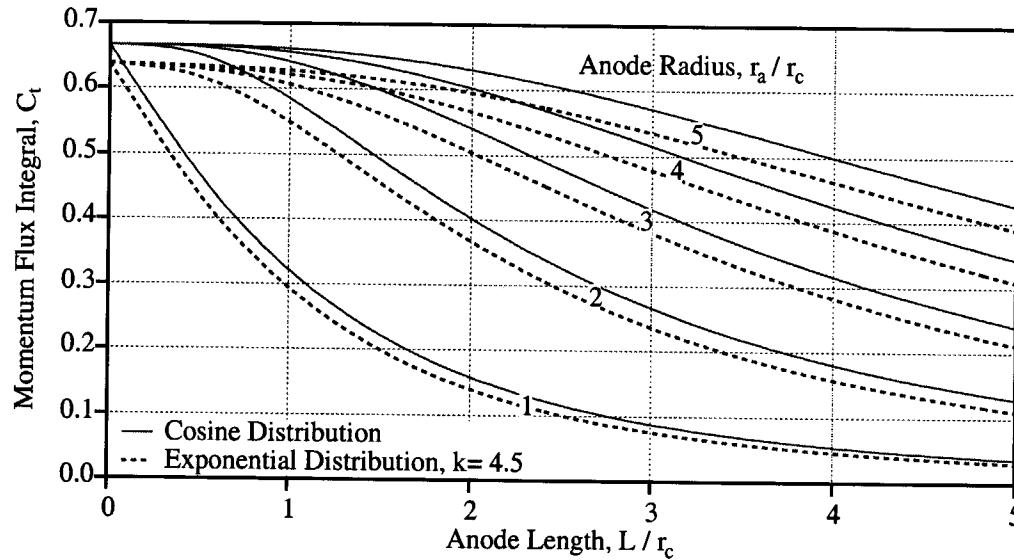
$$F_i = \frac{f_i M_i \langle Z^{-1} \rangle}{e E_r}.$$





# VAT Thrust is Determined by Momentum Flux Through Anode Exit

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Thrust depends on material properties, operating parameters and geometry

$$dT = d\dot{m}_{ip}(l, \phi)(u_i \cos \phi)(\cos \phi dA_2)$$

$$= \frac{M_i j_{ip}}{e} \langle Z^{-1} \rangle u_i \cos^2 \phi dA_2$$

$$T = \frac{M_i f_i J_d u_i}{e} \langle Z^{-1} \rangle C_t(\bar{L}, \bar{r}_a)$$

$$C_t = \frac{\bar{L}^3}{\pi^2} \int_0^{2\pi} \int_0^{2\pi} \int_0^{\bar{r}_a} \int_0^1 \frac{\bar{r}_1 \bar{r}_2 d\bar{r}_1 d\bar{r}_2 d\theta_1 d\theta_2}{\bar{l}^5}$$

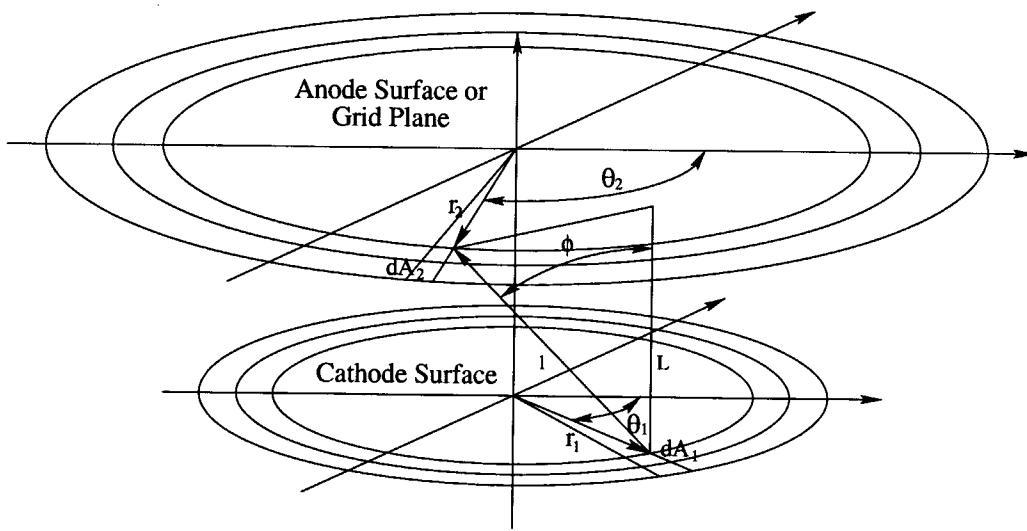
Additional performance parameters

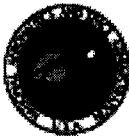
$$I_{sp} = \frac{T}{\dot{m}_t g} = \frac{M_i f_i u_i C_t}{e E_r g} \langle Z^{-1} \rangle$$

$$= \frac{F_i u_i C_t}{g}$$

$$\eta = \frac{T^2}{2\dot{m}_t P} = \frac{M_i^2 f_i^2 u_i^2 C_t^2 (\langle Z^{-1} \rangle)^2}{2e^2 E_r V_d}$$

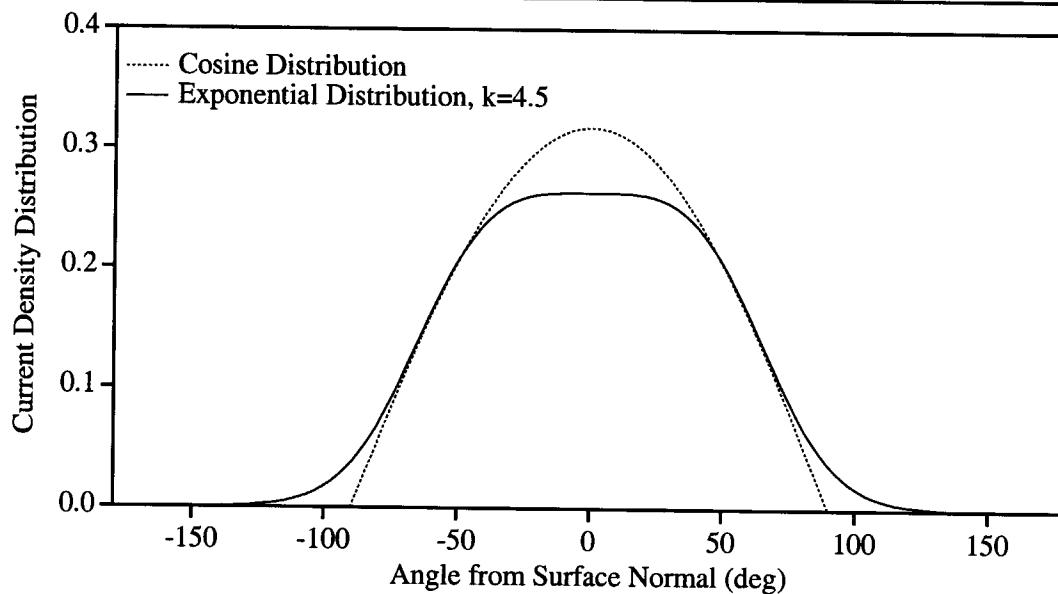
$$T/P = \frac{M_i f_i u_i C_t}{e V_d} \langle Z^{-1} \rangle$$





# Angular Distribution of Ion Current

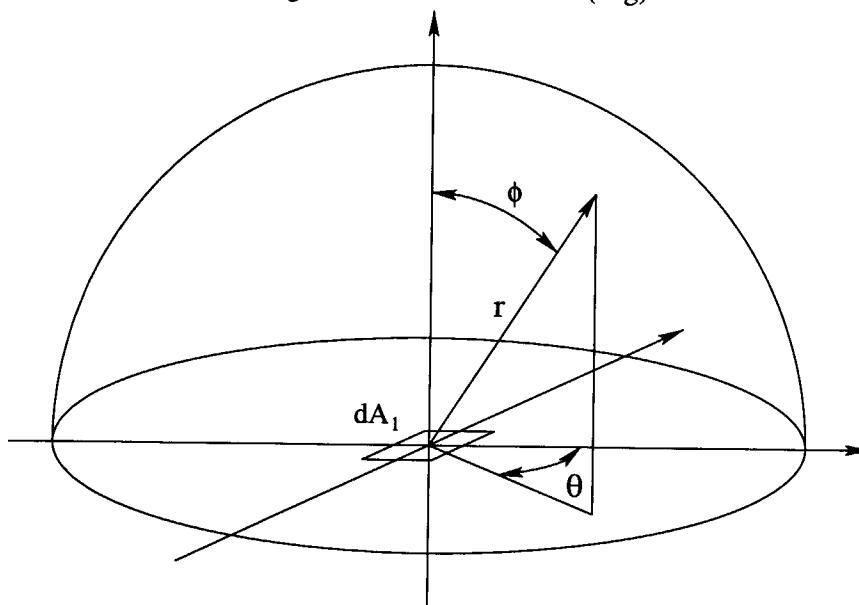
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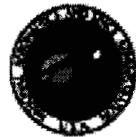


- Experiments show either a cosine or exponential distribution of ion current

$$j_{ip}(l, \phi) = \frac{j_{ic} \cos \phi dA_1}{\pi l^2}$$

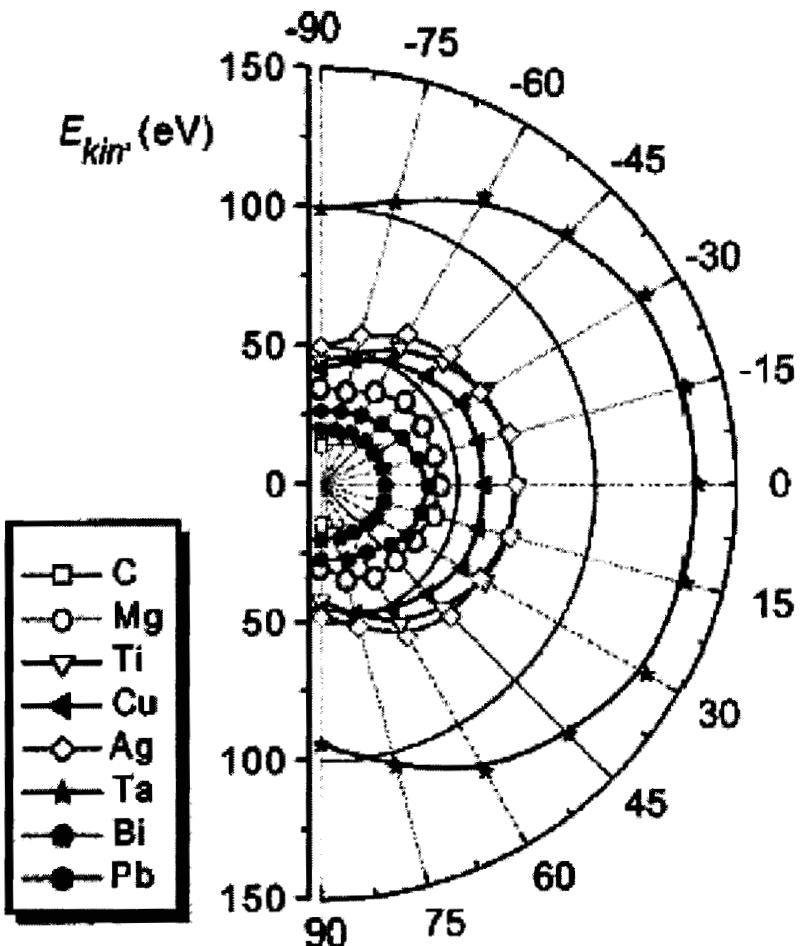
$$j_{ip}(l, \phi) = \frac{2j_{ic} dA_1}{\sqrt{\pi} l^2 k \operatorname{erf}(2\pi/k)} \times \exp(-[2\pi(1 - \cos \phi)]^2/k^2)$$





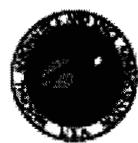
# Angular Distribution of Ion Energy

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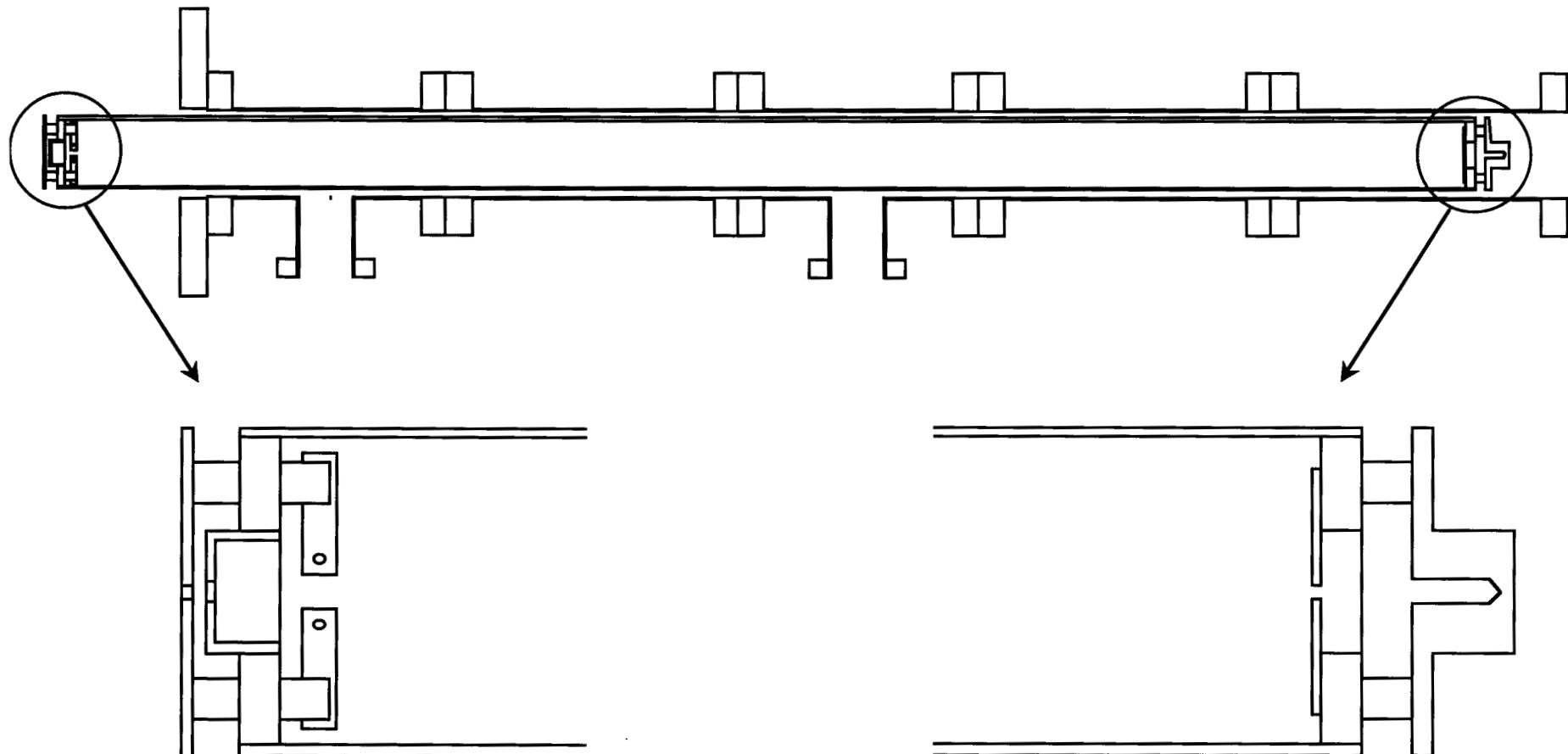
Ion energy is not a strong function of angle, as assumed in the model

Anders, A., and Yushkov, G., "Angularly resolved measurements of ion energy of vacuum arc plasmas," Appl. Phys. Lett., 80(14), pp. 2457-2459, April 8, 2002.



# Time-of-Flight Mass Spectrometer

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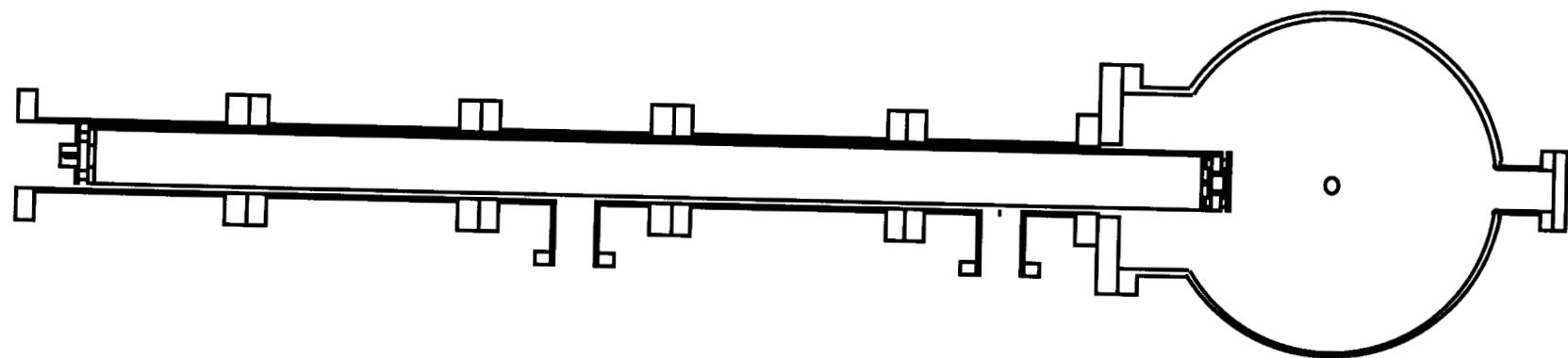
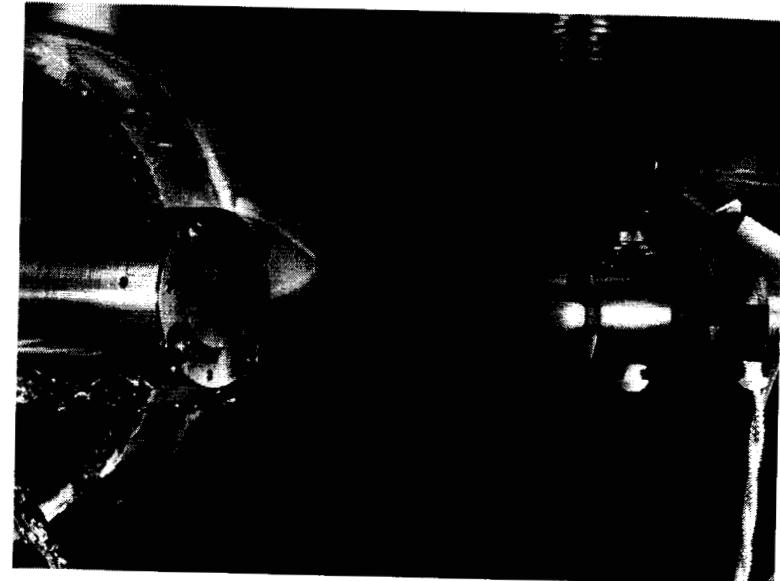
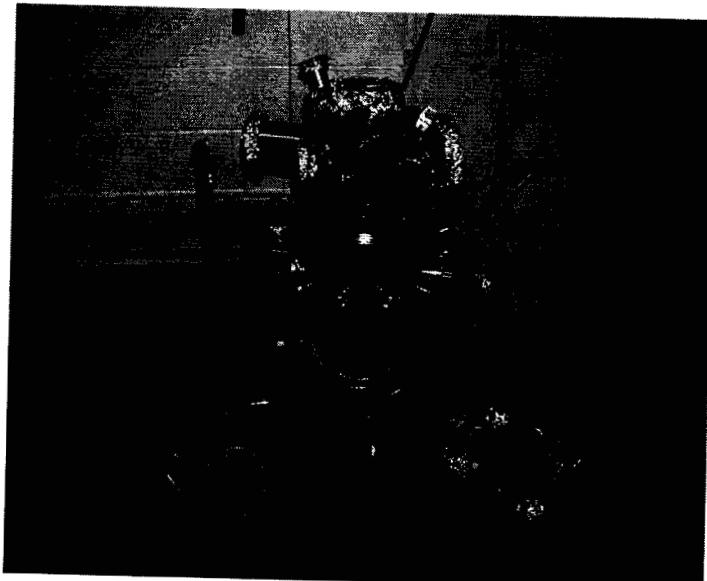
Inlet accelerator and gate electrodes

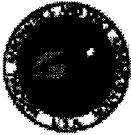
Exit aperture and collector cup



# Vacuum Arc Thruster Test Chamber and Mass Spectrometer

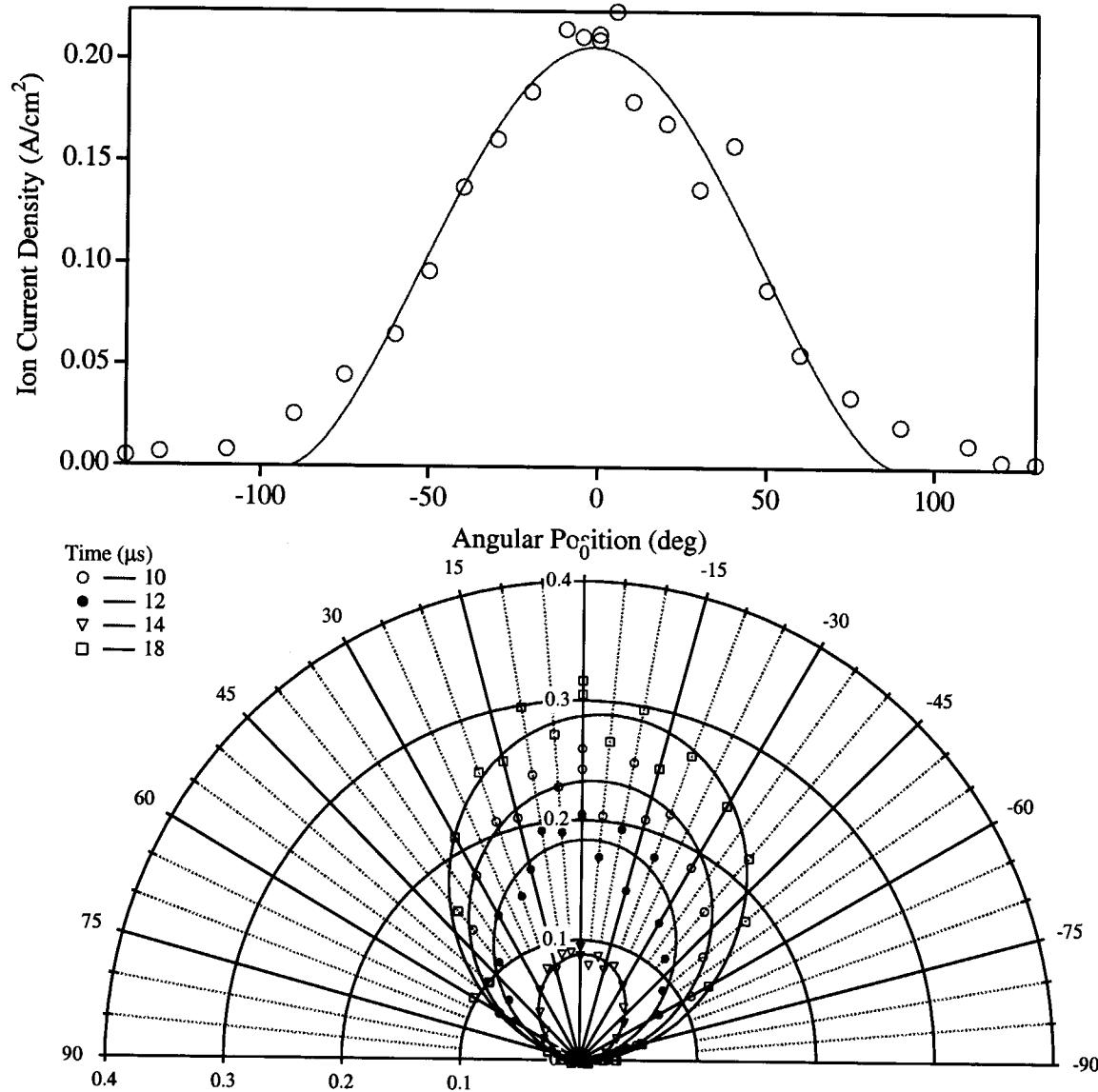
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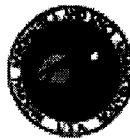




# Angular Distribution of Charge State

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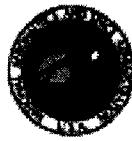




# Material Properties Used to Estimate VAT and VAIT Performance Potential

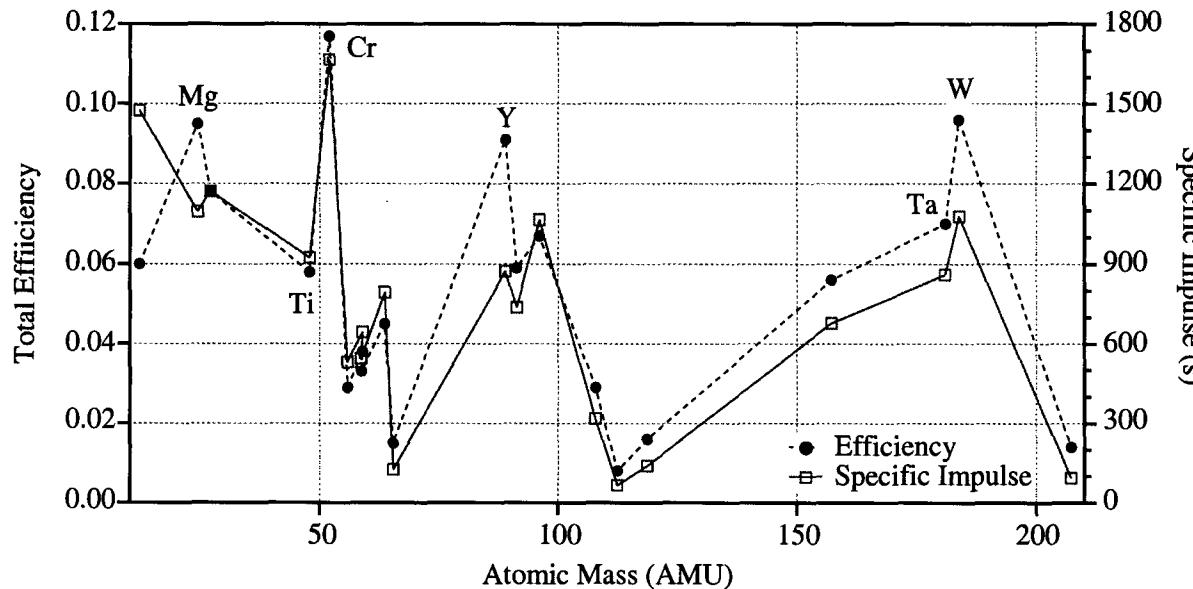
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Species	Mass $M_i$ (AMU)	Ion Charge State Distribution							Erosion Rate $E_r$ ( $\mu\text{g/C}$ )	Ion Fraction $F_i$	Discharge Voltage $V_d$ (V)	Ion Velocity $u_i$ (m/s)
		$f_1$	$f_2$	$f_3$	$f_4$	$f_5$	$f_6$	$\langle Z^{-1} \rangle$	$\langle Z^{-1/2} \rangle$			
Li	6.941	1.000						1.00	1.00			23.5
C	12	1.000						1.00	1.00	17	0.732	29.6
Mg	24.305	0.307	0.701					0.66	0.80	31	0.528	18.8
Al	26.981	0.224	0.590	0.191				0.58	0.75	28	0.577	30600
Si	28.086	0.450	0.504	0.043				0.72	0.83			23.6
Ca	40.08	0.042	0.943	0.016				0.52	0.72			27.5
Sc	44.96	0.150	0.749	0.101				0.56	0.74			23.5
Ti	47.9	0.052	0.739	0.207				0.49	0.69	30	0.815	19.1
V	50.94	0.038	0.664	0.280	0.019			0.47	0.68			21.3
Cr	52	0.048	0.638	0.296	0.019			0.47	0.68	20	1.265	22.5
Mn	54.94	0.327	0.658	0.020				0.66	0.80			22
Fe	55.85	0.139	0.747	0.115				0.55	0.73	48	0.663	10800
Co	58.93	0.200	0.682	0.121				0.58	0.75	44	0.802	22.7
Ni	58.71	0.167	0.727	0.102				0.56	0.74	47	0.736	11800
Cu	63.55	0.080	0.612	0.291	0.019			0.49	0.69	35	0.914	20.5
Zn	65.38	0.667	0.333					0.83	0.90	320	0.176	12800
Ge	69.74	0.429	0.571					0.71	0.83			15.5
Sr	87.62	0.010	0.990					0.50	0.71			17.5
Y	88.91	0.022	0.544	0.434				0.44	0.66	45	0.898	18.1
Zr	91.22	0.004	0.364	0.523	0.109			0.39	0.62	53	0.691	14300
Nb	92.91	0.003	0.160	0.510	0.293	0.033		0.33	0.57			27
Mo	95.94	0.006	0.137	0.480	0.327	0.049		0.33	0.57	36	0.903	15500
Pd	106.4	0.121	0.713	0.144	0.021			0.53	0.72			21.3
Ag	107.87	0.062	0.570	0.350	0.019			0.47	0.68	140	0.373	15700
Cd	112.41	0.523	0.485					0.77	0.87	620	0.142	12500
In	114.82	0.471	0.507					0.73	0.83			16
Sn	118.69	0.313	0.693					0.66	0.80	295	0.273	5500
Ba	137.33	0.000	1.000					0.50	0.71			17.5
La	138.91	0.005	0.685	0.311				0.45	0.67			7500
Ce	140.12	0.014	0.787	0.199				0.47	0.69			18.3
Pr	140.91	0.014	0.613	0.373				0.44	0.66			17.2
Nd	144.24		0.765	0.235				0.46	0.68			20
Sm	150.4	0.010	0.779	0.211				0.47	0.68			8700
Gd	157.25	0.009	0.691	0.300				0.45	0.67	55	1.347	19.8
Dy	162.5	0.009	0.574	0.417				0.43	0.66			7400
Ho	164.93	0.009	0.574	0.417				0.43	0.66			21.6
Er	167.26	0.004	0.534	0.445	0.017			0.42	0.65			22.5
Yb	173.04	0.014	0.867	0.118				0.49	0.70			14.4
Hf	178.49	0.010	0.164	0.522	0.287	0.017		0.34	0.58			9200
Ta	180.95	0.007	0.225	0.389	0.328	0.051		0.34	0.58	56	1.143	11100
W	183.85	0.006	0.147	0.413	0.333	0.080	0.019	0.32	0.56	55	1.111	4200
Ir	192.22	0.019	0.278	0.519	0.165	0.019		0.38	0.61			31.9
Pt	195.09	0.057	0.663	0.260	0.019			0.48	0.69			14.4
Au	196.97	0.070	0.761	0.168				0.51	0.71			5800
Pb	207.2	0.225	0.780					0.62	0.78	510	0.257	15.5
Bi	208.98	0.692	0.291					0.84	0.90			5400
Th	232.04	0.000	0.166	0.124	0.166			0.17	0.27			15.6
U	231.04	0.075	0.547	0.377				0.31	0.56			9900



# VATs Show Promise as Simple, Miniature Pulsed Thrusters

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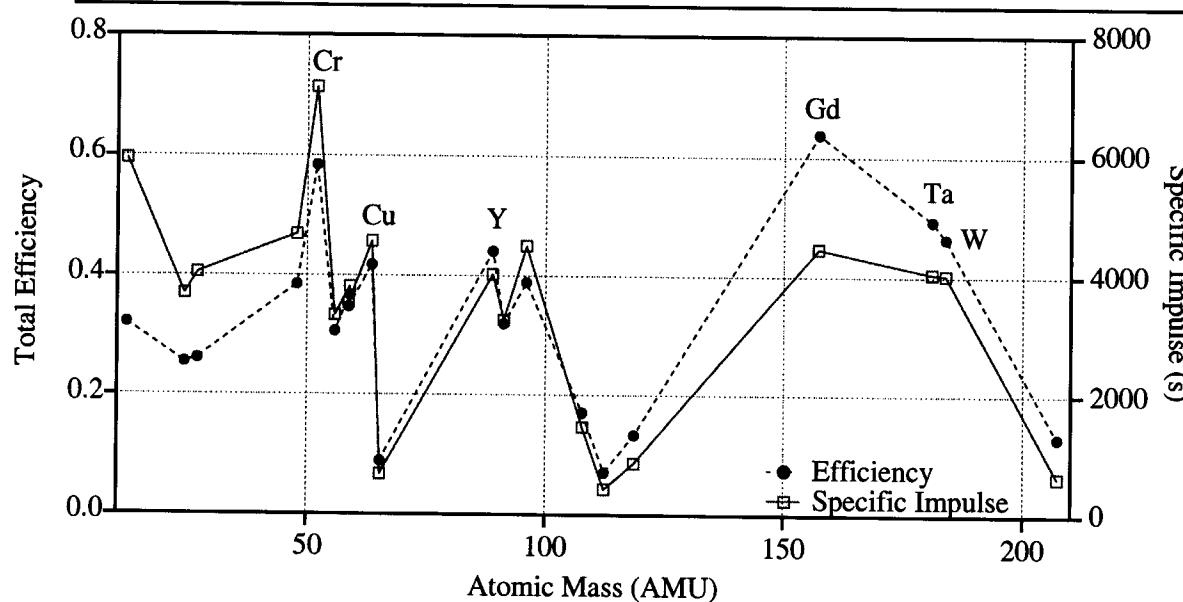
- Assumptions:
  - $J_d = 10 \text{ A}$
  - $f_i = 0.1$
  - $C_t = 0.666$
- Cr, Gd, Ta and W have unrealistically high values of ion mass fraction
  - $f_i < 0.1$
  - $E_r > \text{measured values}$

Species	Erosion Rate, $E_r$ ( $\mu\text{g/C}$ )	Ion Current Fraction $f_i$	Ion Mass Fraction $F_i$	Vacuum Arc Thruster			Vacuum Arc Ion Thruster		
				$I_{sp}$ (s)	Total Efficiency $\eta$	Thrust-to-Power $T/P$ ( $\mu\text{N/W}$ )	$I_{sp}$ (s)	Propellant Efficiency $\eta_u$	Total Efficiency $\eta$
Cr	20	0.100	1.265	1666	0.117	14.3	7143	0.81	0.585
	20	0.079	1.000	1316	0.073	11.3	5643	0.64	0.432
	25.3	0.100	1.000	1317	0.092	14.3	5647	0.64	0.462
Gd	55	0.100	1.347	677	0.056	16.9	4464	0.86	0.638
	55	0.074	1.000	501	0.031	12.5	3304	0.64	0.434
	74	0.100	1.000	503	0.042	16.9	3319	0.64	0.474
Ta	56	0.100	1.143	861	0.070	16.5	4050	0.73	0.493
	56	0.087	1.000	749	0.053	14.4	3523	0.64	0.410
	64	0.100	1.000	754	0.061	16.5	3544	0.64	0.432
W	55	0.100	1.111	1078	0.096	18.2	4029	0.71	0.464
	55	0.090	1.000	970	0.078	16.4	3626	0.64	0.402
	61	0.100	1.000	972	0.087	18.2	3632	0.64	0.418

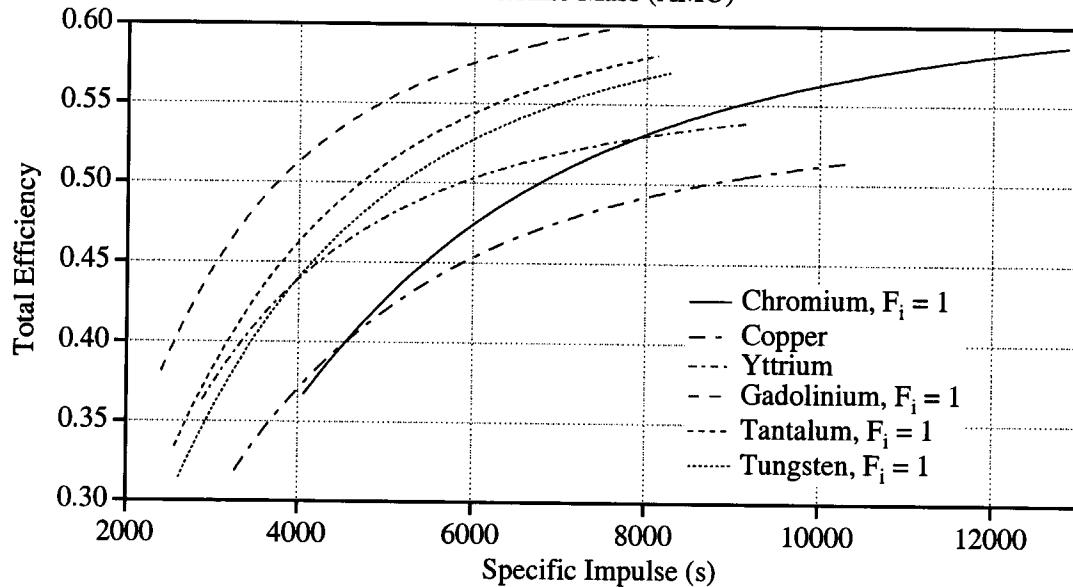


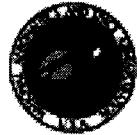
# VAITs Offer Much Higher Performance Capability

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- Assumptions:
  - $J_d = 10 \text{ A}$
  - $f_i = 0.1$
  - $C_j = 0.8$
  - Transparency = 0.8
  - $V_b = 1000 \text{ V}$
- Performance can be improved by increasing beam voltage





## Conclusions

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- 
- A time-of-flight mass spectrometer adequately resolves the angular distribution of charge states in the plume of a vacuum arc thruster
  - Charge state distributions measured for titanium agree well with measurements from Lawrence Berkeley National Laboratory
  - The results indicate that the charge state does not vary dramatically with angle
  - Models of vacuum arc thruster performance are not significantly affected by angular variation in charge state distribution